

The Scale of Dark QCD

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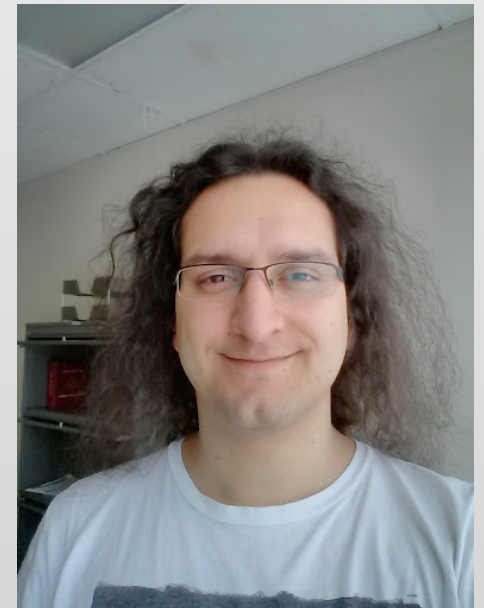
Lattice Meets Experiment 2013

arXiv: 1306.4676

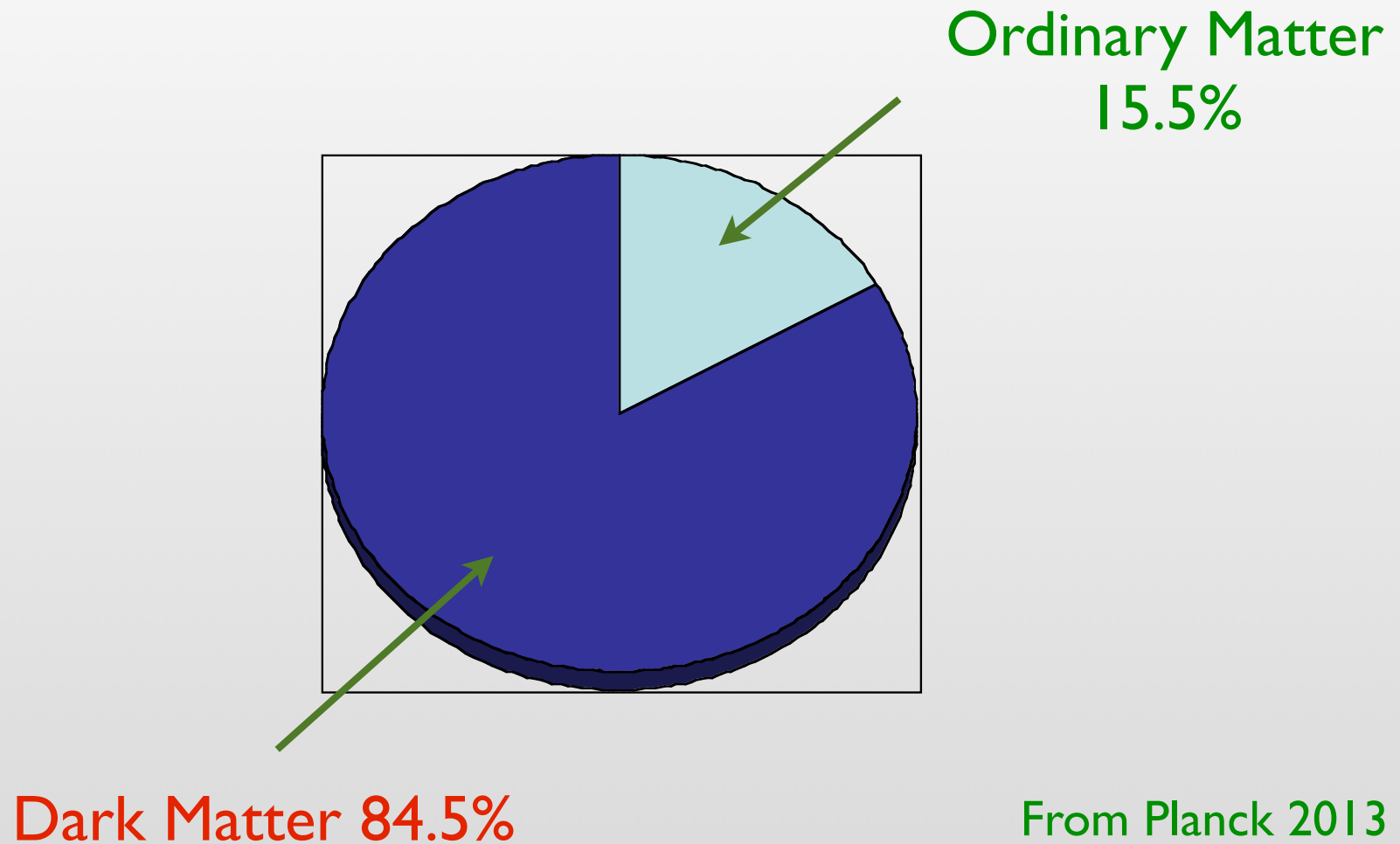
with **Pedro Schwaller**

at CERN

Dec. 5, 2013



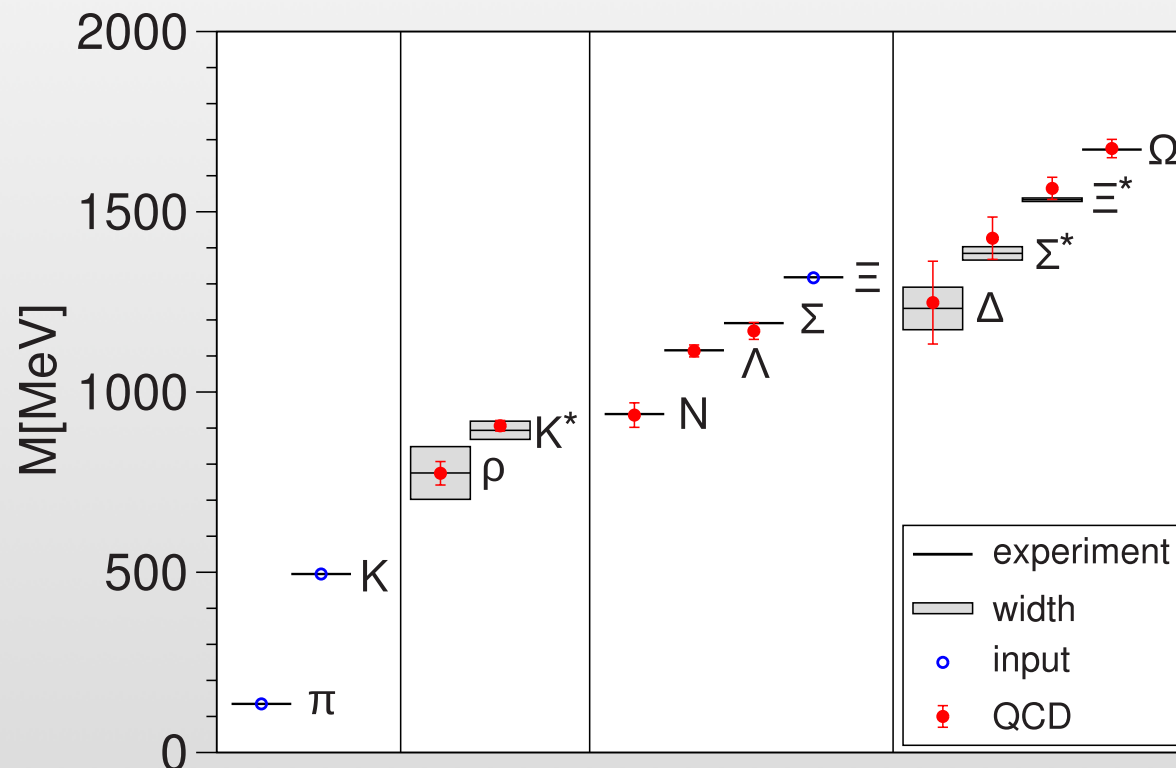
Dark Matter Energy Density



Ordinary Matter

The ordinary matter has its mass from protons and neutrons

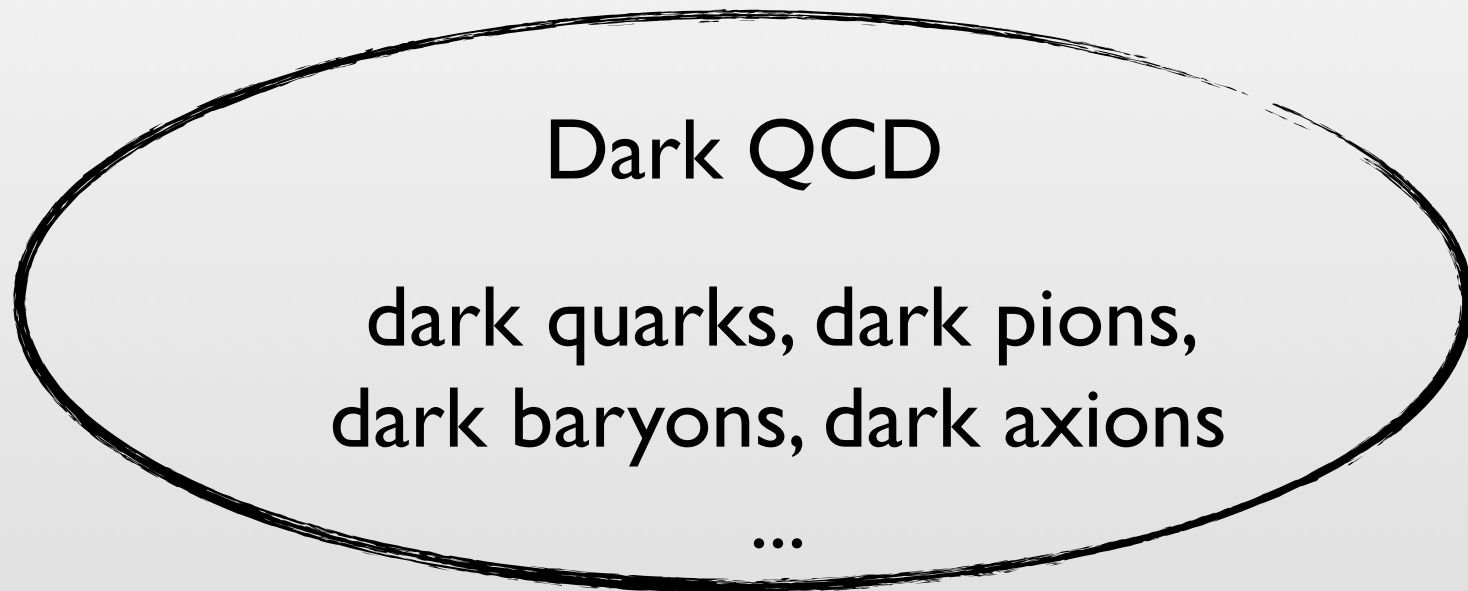
Durr, et.al., Science 322, 1224 (2008)



90% of the mass of ordinary matter emerges from QCD

Introduction of Dark QCD

A simple-minded conjecture:



The dark matter has its mass from a “dark QCD”

Is it new?

TECHNOCOSMOLOGY – COULD A TECHNIBARYON EXCESS PROVIDE A “NATURAL” MISSING MASS CANDIDATE?

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Received 7 October 1985

asymmetric dark matter

TECHNICOLOR COSMOLOGY

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Terry P. WALKER

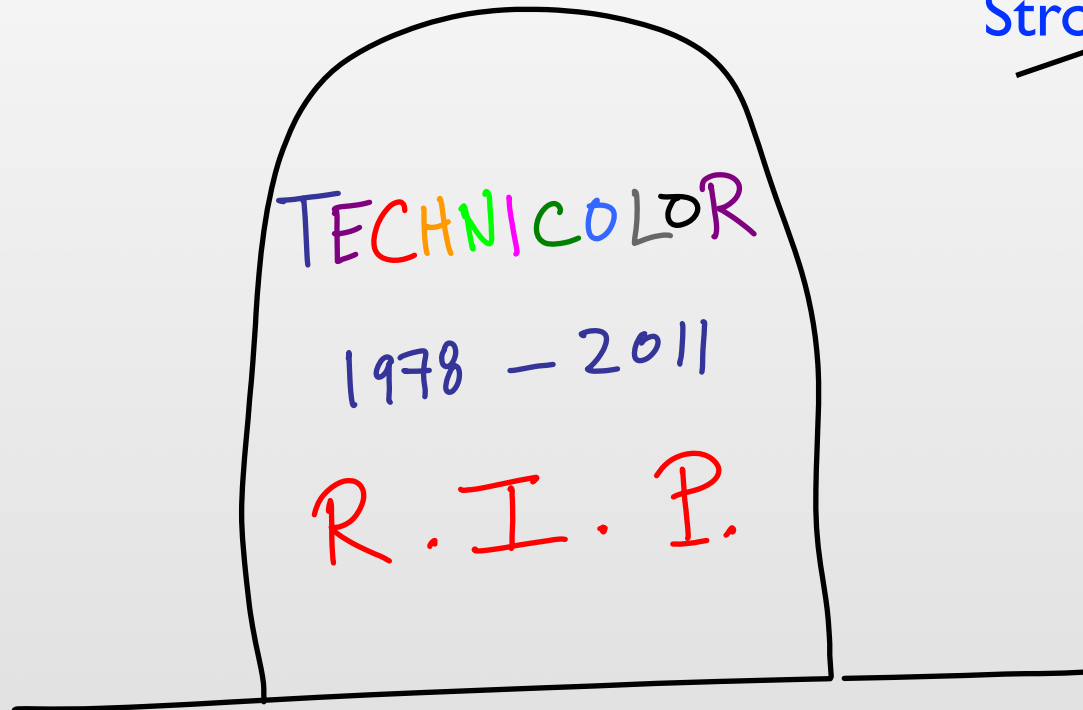
Harvard-Smithsonian Center for Astrophysics, Cambridge, MA 02138, USA

Received 16 June 1989

WIMP

The Discovery of Higgs Boson

~~Strong dynamics~~



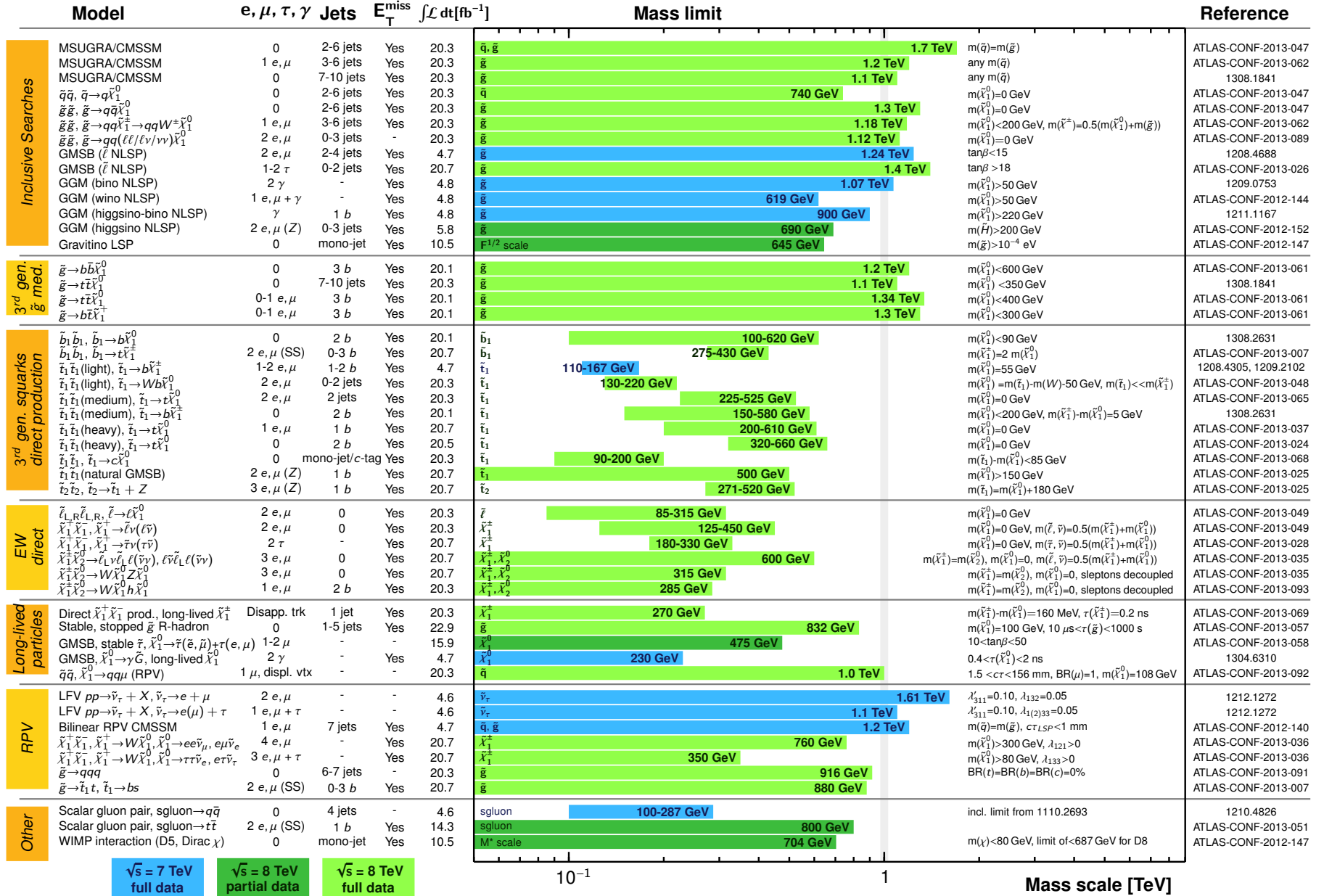
Nima Arkani-Hamed, talk at SavasFest, May 2012

ATLAS SUSY Searches* - 95% CL Lower Limits

Status: SUSY 2013

ATLAS Preliminary

$$\int \mathcal{L} dt = (4.6 - 22.9) \text{ fb}^{-1} \quad \sqrt{s} = 7, 8 \text{ TeV}$$



*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1σ theoretical signal cross section uncertainty.

we've seen this
for a while



time to add this?



some talk given by someone in the audience

The dynamics in the dark sector may have nothing to do with the electroweak symmetry breaking !!!

We need to study dark matter for its own purpose

One Number to Explain

$$\frac{\Omega_{\text{DM}}}{\Omega_{\text{Baryon}}} = \frac{m_{\text{DM}} n_{\text{DM}}}{m_p n_p} \approx 5 \sim 6$$

Most popular models: “WIMP miracle”

$$\Omega_{\text{DM}} = \frac{s_0}{\rho_c} \left(\frac{45}{\pi g_*} \right)^{1/2} \frac{x_f}{m_{\text{pl}}} \frac{1}{\langle \sigma v \rangle} \quad \langle \sigma v \rangle \approx 1 \text{ pb} \approx \frac{\pi \alpha^2}{8 m_{\text{DM}}^2}$$

for $m_{\text{DM}} = 100 \text{ GeV}$

This could be just one option:

dark matter is related to the electroweak scale

Two Options in dark QCD

- Thermal dark matter (not necessarily weakly-interaction)

$$\langle\sigma v\rangle \approx 1 \text{ pb} \qquad \langle\sigma v\rangle \approx \frac{g_\chi^4}{4\pi m_{\text{DM}}^2} \approx \frac{(4\pi)^2}{4\pi m_{\text{DM}}^2}$$

- Asymmetric dark matter

$$\frac{\Omega_{\text{DM}}}{\Omega_{\text{Baryon}}} = \frac{m_{\text{DM}} n_{\text{DM}}}{m_p n_p} \approx 5 \sim 6$$

Two conditions:

(1): $n_{\text{DM}} \sim n_p$

(2): $m_{\text{DM}} \sim m_p$

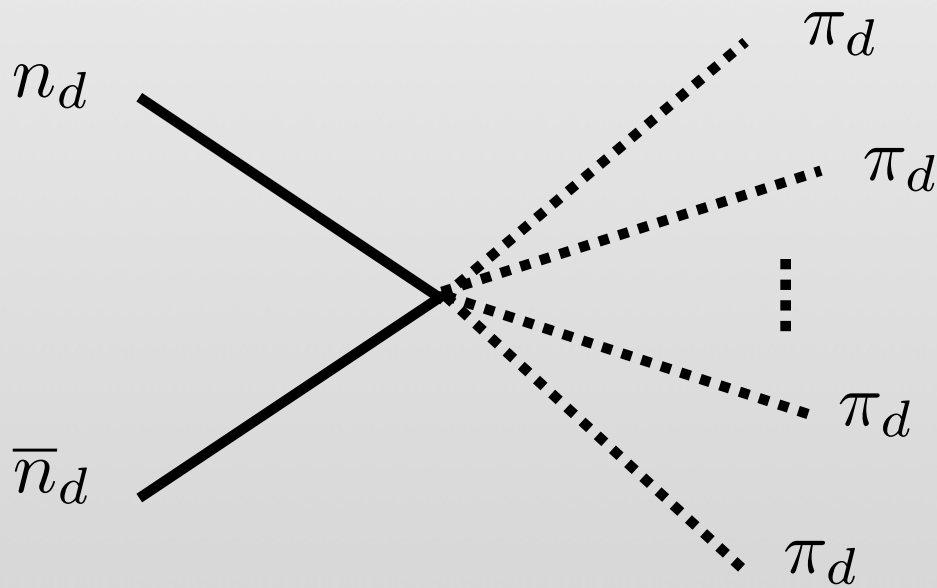
Thermal Dark Baryon

- For simplicity, we just use $SU(N_d = 3)$ as dark QCD gauge group. With two flavors of dark quarks, the “dark neutron” could be the dark matter candidate

It is a Dirac dark fermion:

general study for Dirac DM:
Harnik and Kribs: 0810.5557

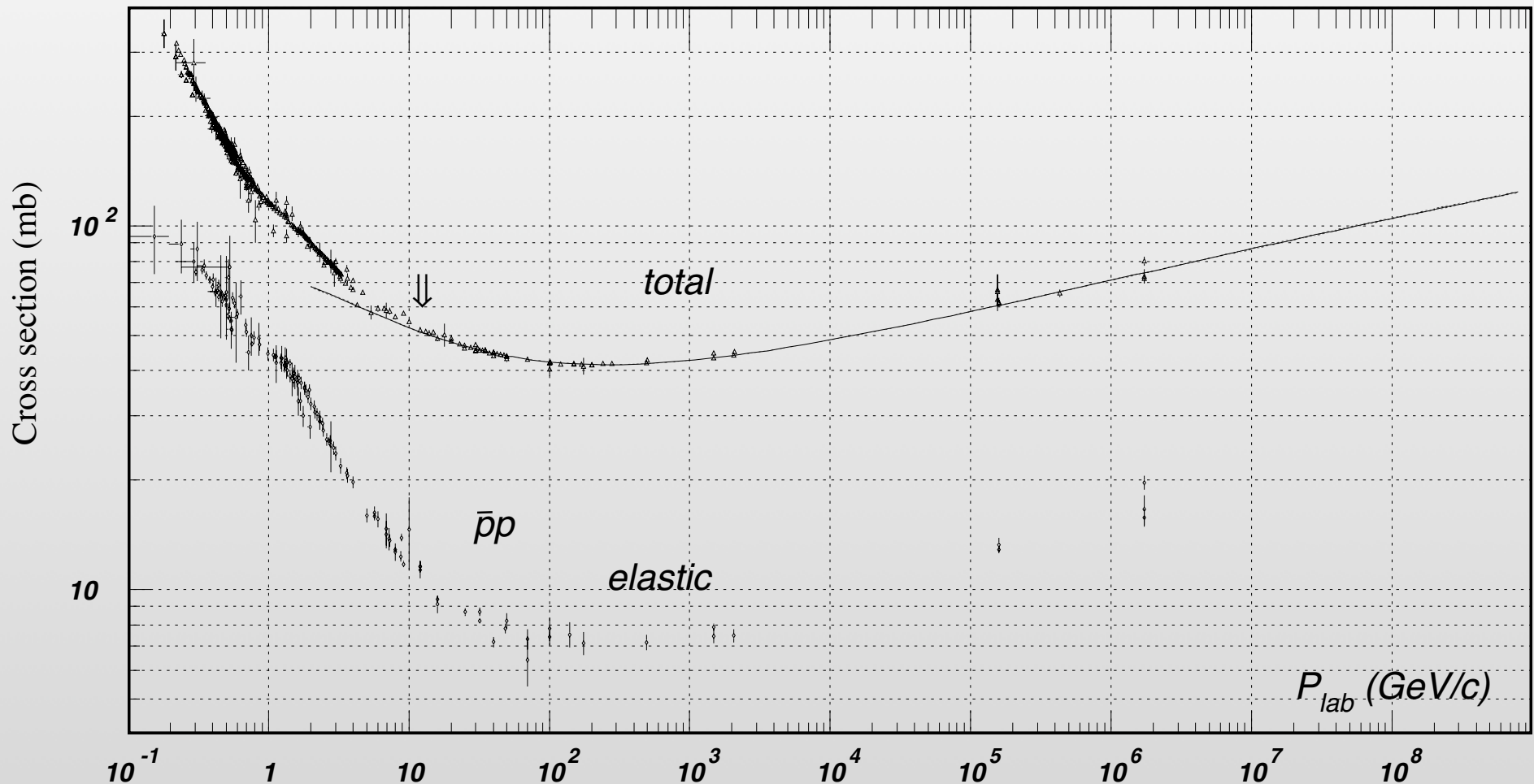
It is not p-wave suppressed; however:



π_d then decays
to SM particles

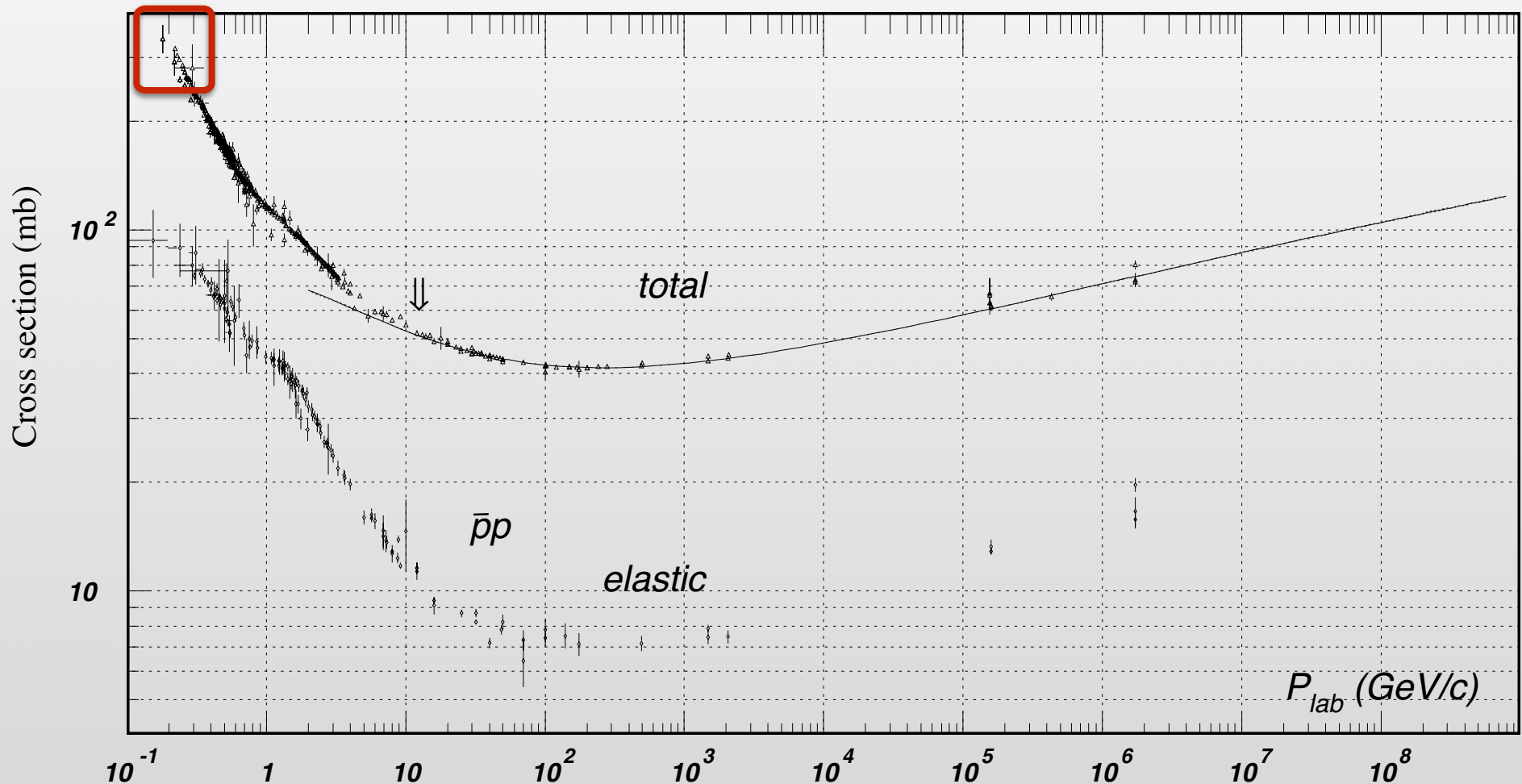
Thermal Dark Baryon

- Fortunately, we have experimental data from our QCD sector



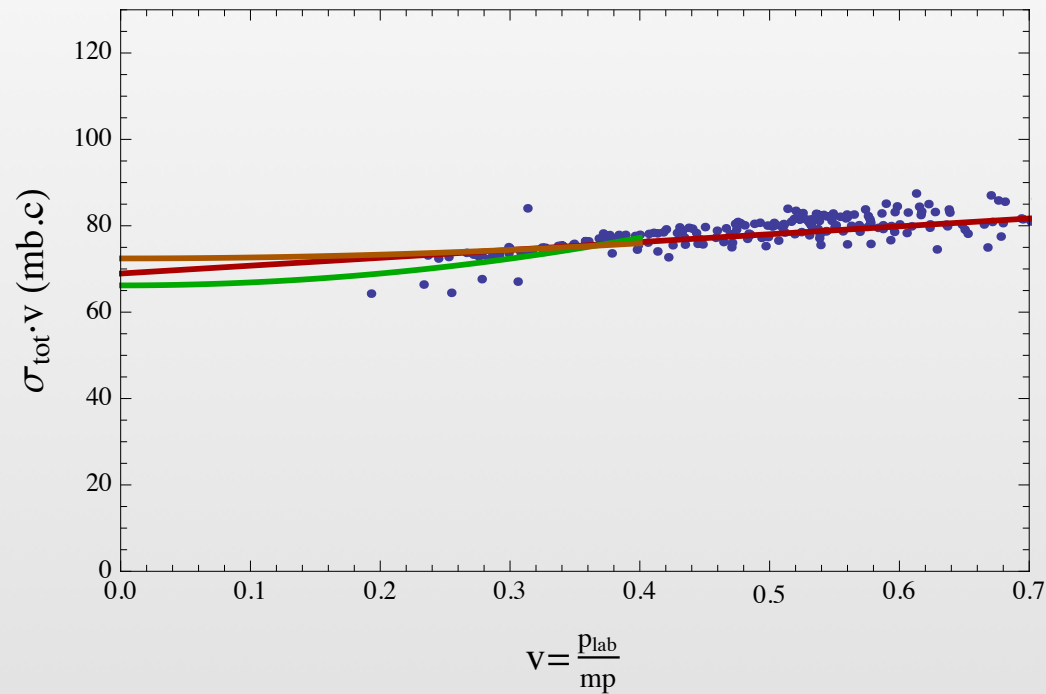
Thermal Dark Baryon

- Fortunately, we have experimental data from our QCD sector



Thermal Dark Baryon

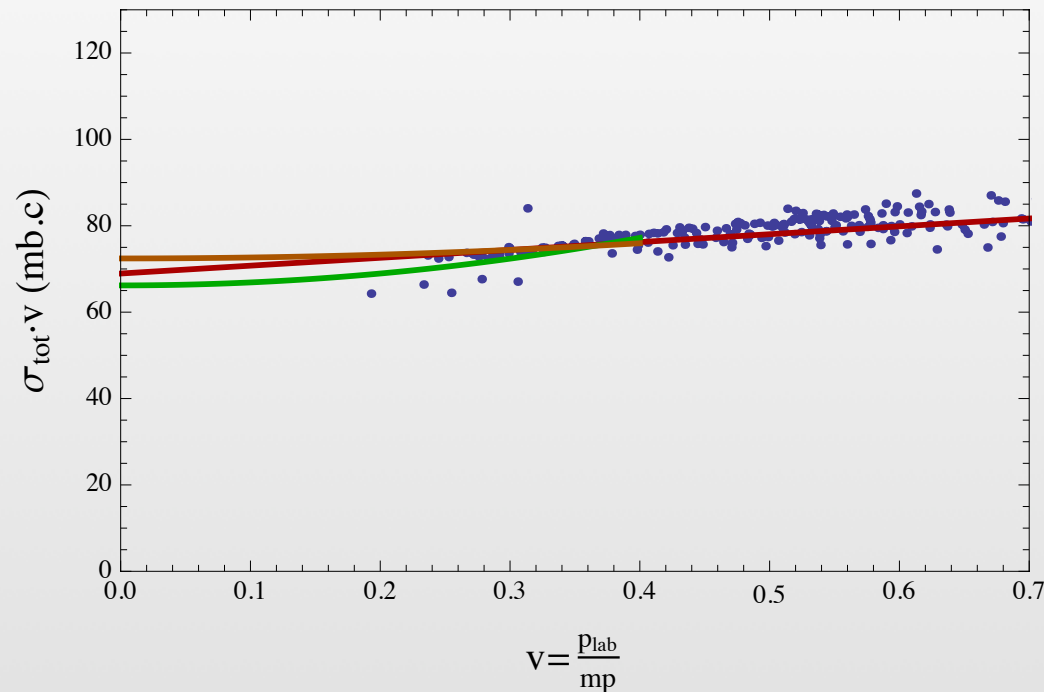
- Use polynomial to fit the data YB, Draper, Lu, in progress



$$(\sigma \cdot v)_{n_d \bar{n}_d} = (\sigma \cdot v)_{p\bar{p}} \frac{m_p^2}{m_{\text{dark neutron}}^2}$$

Thermal Dark Baryon

- Use polynomial to fit the data YB, Draper, Lu, in progress



$$(\sigma \cdot v)_{n_d \bar{n}_d} = (\sigma \cdot v)_{p\bar{p}} \frac{m_p^2}{m_{\text{dark neutron}}^2}$$

relic abundance
calculation



$$m_{\text{dark neutron}} \approx 150 \text{ TeV}$$

Thermal Dark Baryon

- Too high for the current hadron colliders
- Direct detection can still probe the thermal dark neutron

a) Tree-level coupling to Z boson

b) Dimension-5 operator:

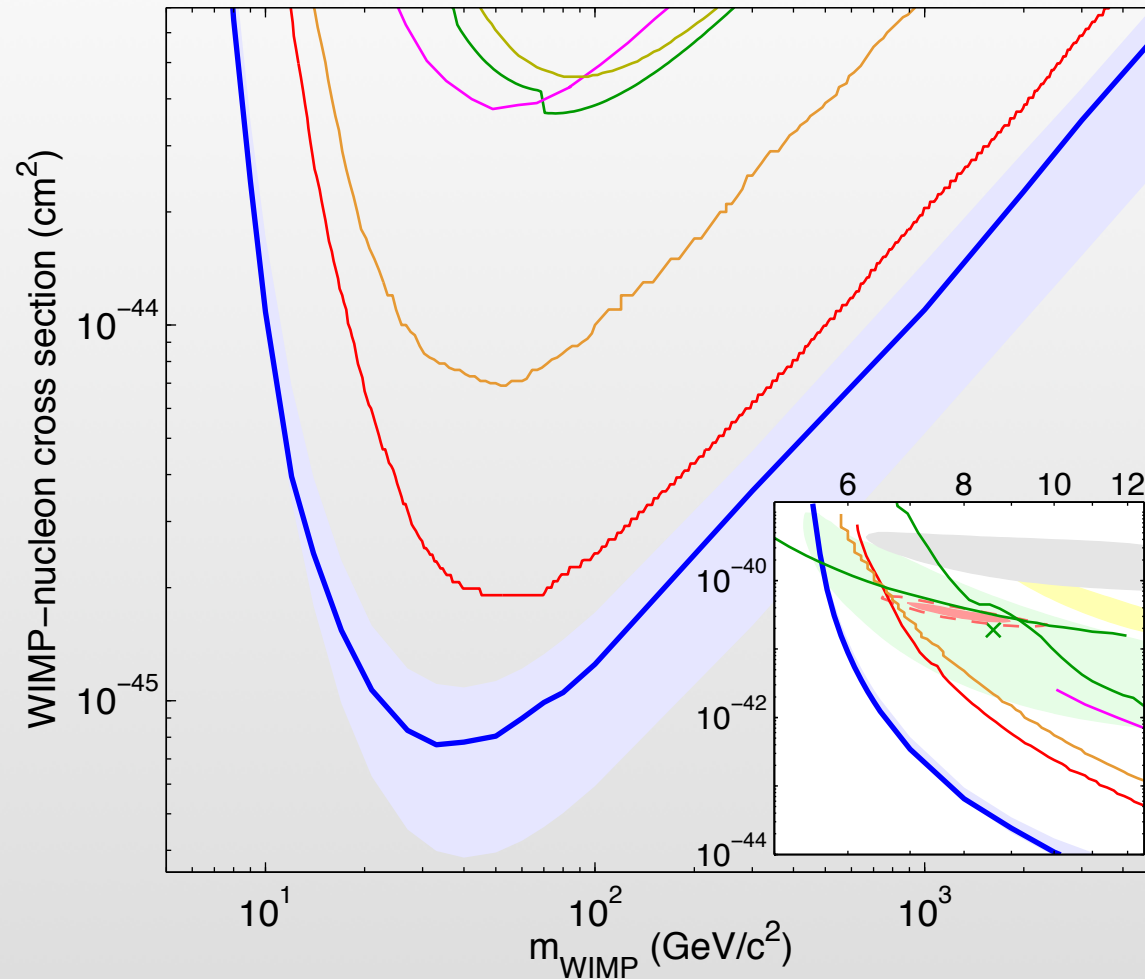
LSD collaboration,
1301.1693

$$\frac{e}{\Lambda_{\text{dQCD}}} \bar{n}_d \sigma^{\mu\nu} n_d F_{\mu\nu}$$

c) Dimension-7 operator:

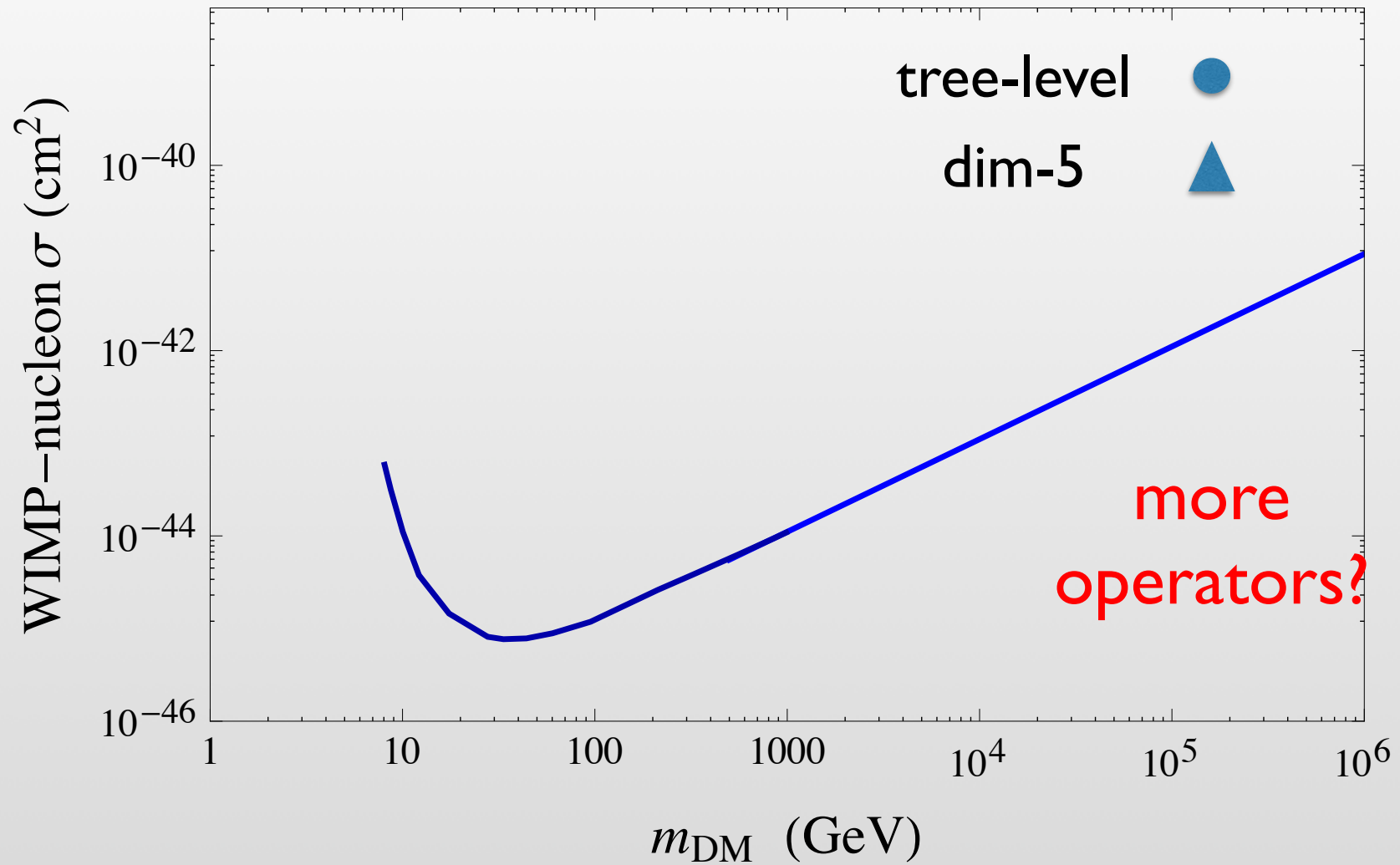
$$\frac{g_s^2}{\Lambda_{\text{dQCD}}^3} \bar{n}_d n_d (G_{\mu\nu}^a)^2$$

Direct Detection from LUX



at higher masses, the limits become weaker and are proportional to the dark matter mass

Direct Detection from LUX



dim-7



- Thermal dark matter
- Asymmetric dark matter

$$\frac{\Omega_{\text{DM}}}{\Omega_{\text{Baryon}}} = \frac{m_{\text{DM}} n_{\text{DM}}}{m_p n_p} \approx 5 \sim 6$$

Two conditions:

(1): $n_{\text{DM}} \sim n_p$

(2): $m_{\text{DM}} \sim m_p$

(I): $n_{\text{DM}} \sim n_p$

The first condition can be satisfied by introducing some non-trivial number density history

Barr, Chivukula, Farhi, PLB, 241, 387 (1990)

David B. Kaplan, PRL, 68, 741 (1992)

Dodelson, Greene, Widrow, NPB, 372, 467 (1992)

Fujii, Yanagida, PLB, 542, 80 (2002)

Kitano, Low, PRD, 71, 023510 (2005)

Farrar, Zaharijas, PRL, 96, 041302 (2006)

Gudnason, Kouvaris, Sannino, PRD, 73, 115003 (2006)

Kaplan, Luty, Zurek, PRL, 79, 115016 (2009)

Shelton, Zurek, PRD, 82, 123512 (2010)

Davoudiasl, Morrissey, Sigurdson, Tulin, PRL, 105, 211304 (2010)

Buckley, Randall, JHEP, 1109, 009 (2011)

(2): $m_{\text{DM}} \sim m_p$

The dark matter could be like ordinary baryons from an asymmetry mechanism

The dark matter mass is related to the QCD scale

If dark matter is a “dark baryon” from a new QCD-like strong dynamics in the dark matter sector

$$\Lambda_{\text{dQCD}} \sim \Lambda_{\text{QCD}} \quad ?$$

Need to have QCD and dQCD gauge couplings related to each other

Dimensional Transmutation

$$\Lambda_{\text{QCD}}^2 \approx M_{\text{P1}}^2 e^{4\pi / [\beta_0^s \alpha_s(M_{\text{P1}}^2)]} \quad \beta_0 < 0$$

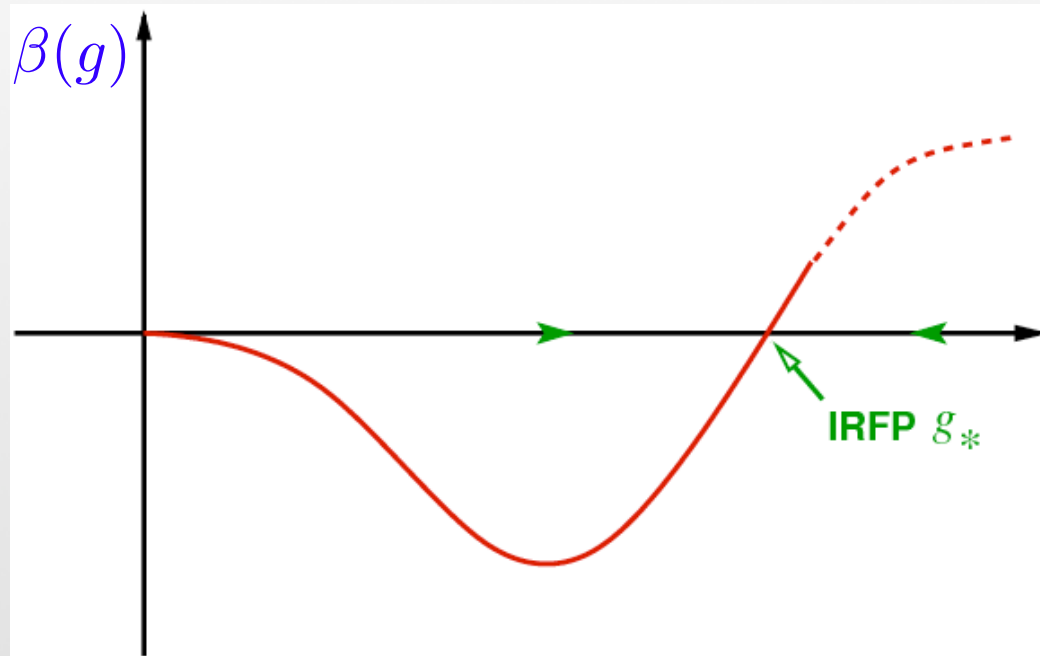
$$\Lambda_{\text{dQCD}}^2 \approx M_{\text{P1}}^2 e^{4\pi / [\beta_0^d \alpha_d(M_{\text{P1}}^2)]}$$

The confinement scale is sensitive to the beta function (matter content) and the coupling at a UV scale

Need a mechanism to relate the gauge couplings of two gauge groups in an infrared scale

Our idea

Banks-Zaks fixed point



Particles charged under both gauge groups can induce Infrared Fixed Points (IRFP) and have both gauge couplings related to each other in the IR

Matter Content

$$G_{\text{gauge}} = SU(N_c)_{\text{QCD}} \times SU(N_d)_{\text{dQCD}}$$

Field	$SU(N_c)_{\text{QCD}}$	$SU(N_d)_{\text{darkQCD}}$	multiplicity
SM fermion	N_c	1	n_{f_c}
SM scalar	N_c	1	n_{s_c}
DM fermion	1	N_d	n_{f_d}
DM scalar	1	N_d	n_{s_d}
joint fermion	N_c	N_d	n_{f_j}
joint scalar	N_c	N_d	n_{s_j}

a general matter content

upper bounds on multiplicities from asymptotic freedom

Gauge Coupling Running

$$\frac{dg_c}{d(\log \mu)} = \beta_c(g_c, g_d),$$

$$\frac{dg_d}{d(\log \mu)} = \beta_d(g_c, g_d)$$

Jones, PRD, 25, 581 (1982)

$$\begin{aligned} \beta_c(g_c, g_d) = & \frac{g_c^3}{16\pi^2} \left[\frac{2}{3} T(R_f) 2(n_{f_c} + N_d n_{f_j}) + \frac{1}{3} T(R_s) (n_{s_c} + N_d n_{s_j}) - \frac{11}{3} C_2(G_c) \right] \\ & + \frac{g_c^5}{(16\pi^2)^2} \left[\left(\frac{10}{3} C_2(G_c) + 2C_2(R_f) \right) T(R_f) 2(n_{f_c} + N_d n_{f_j}) \right. \\ & \quad \left. + \left(\frac{2}{3} C_2(G_c) + 4C_2(R_s) \right) T(R_s) (n_{s_c} + N_d n_{s_j}) - \frac{34}{3} C_2^2(G_c) \right] \\ & + \frac{g_c^3 g_d^2}{(16\pi^2)^2} [2C_2(R_f) T(R_f) 2 N_d n_{f_j} + 4C_2(R_s) T(R_s) N_d n_{s_j}] . \end{aligned}$$

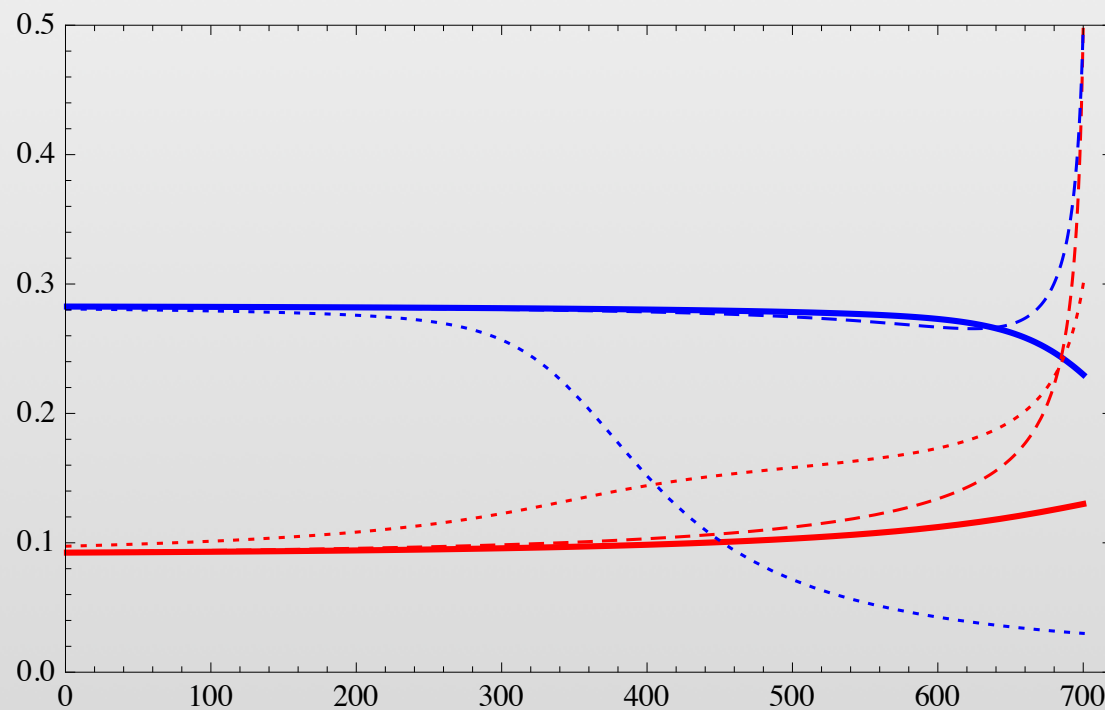
$$c \leftrightarrow d \quad \text{for} \quad \beta_d(g_c, g_d)$$

Infrared Fixed Point

$$\beta_c(g_c, g_d) = \beta_d(g_c, g_d) = 0$$

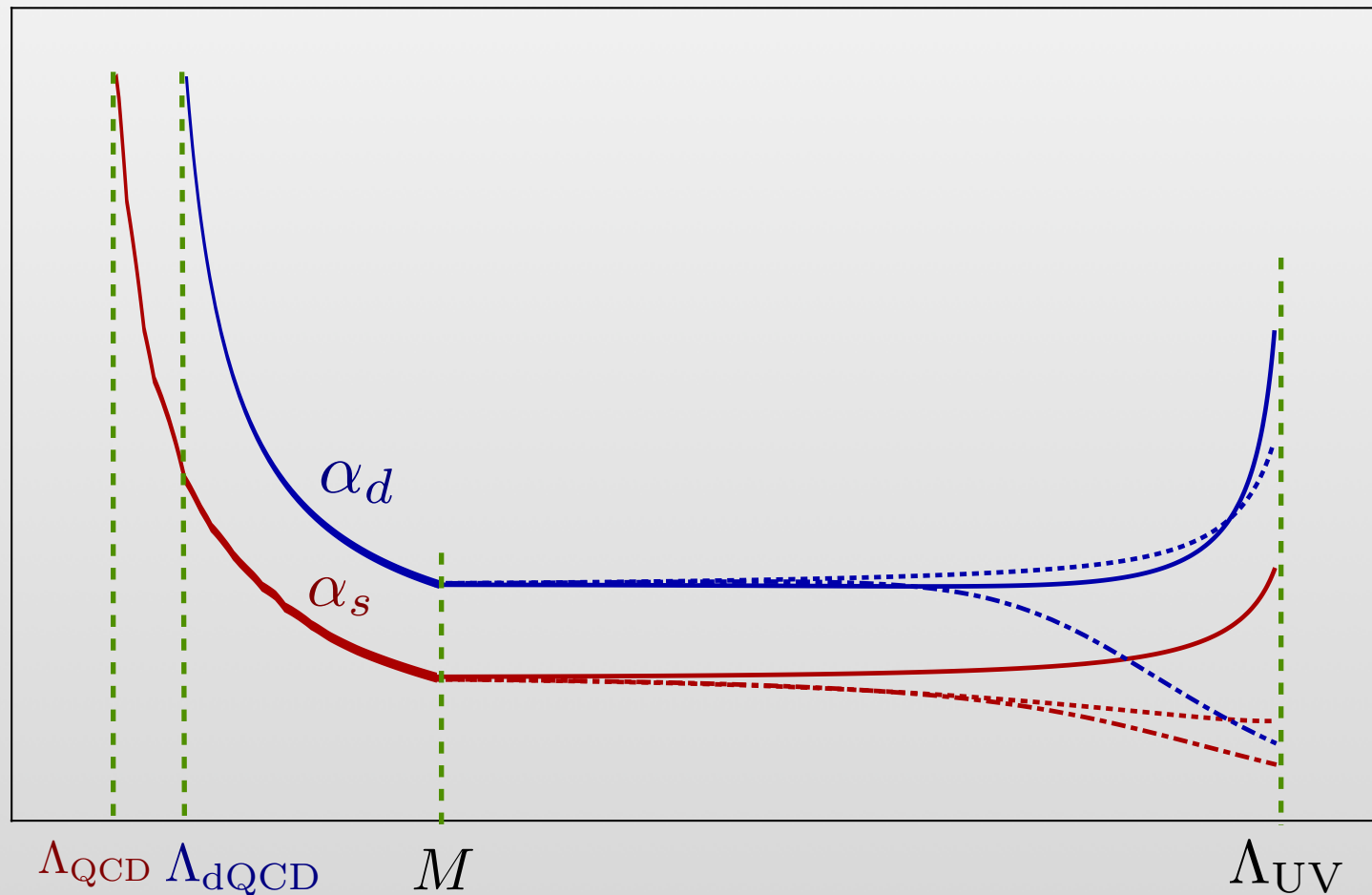
$$\alpha_s^* \equiv \alpha_s^*(n_{f_c}, n_{s_c}, n_{f_d}, n_{s_d}, n_{f_j}, n_{s_j})$$

$$\alpha_d^* \equiv \alpha_d^*(n_{f_c}, n_{s_c}, n_{f_d}, n_{s_d}, n_{f_j}, n_{s_j})$$

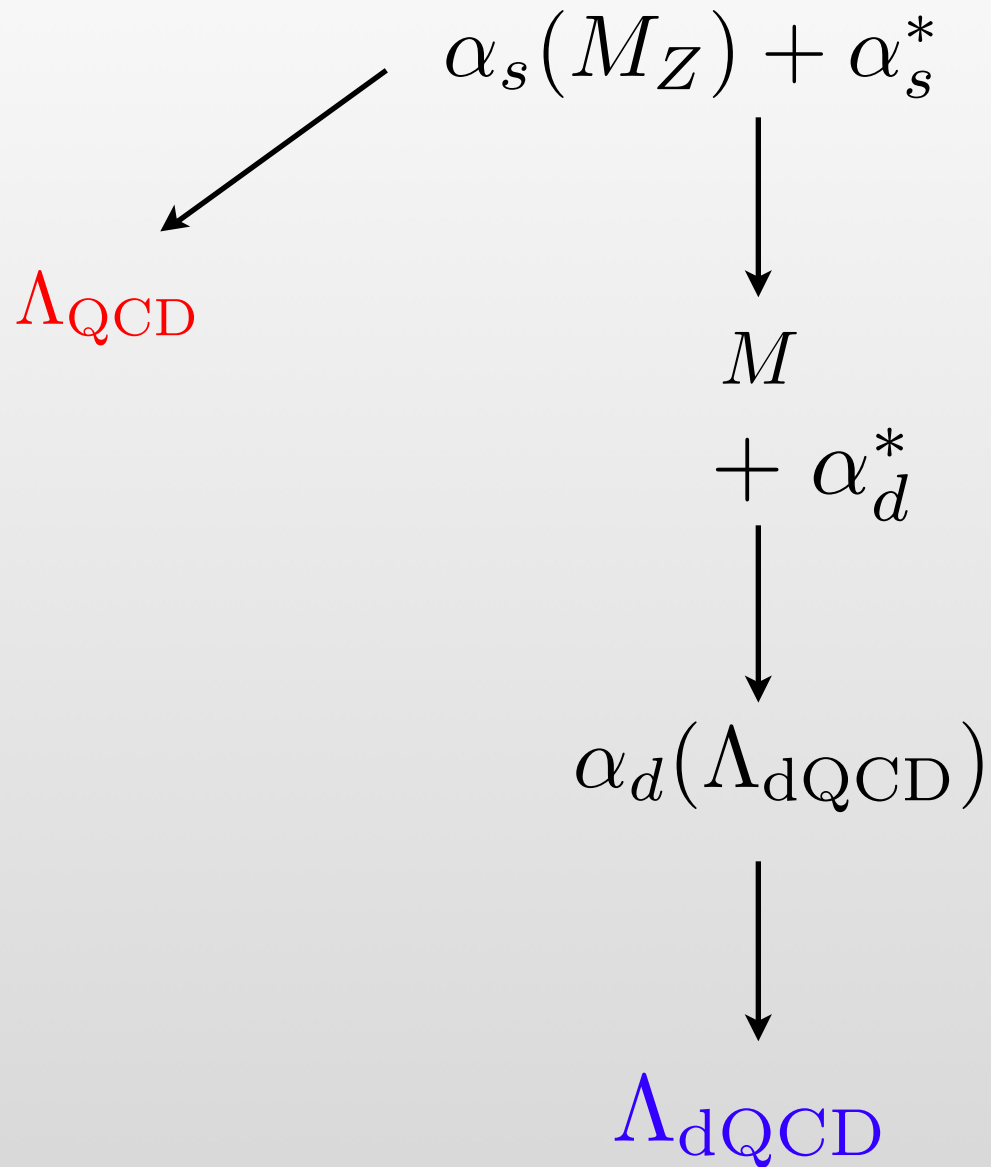


Dark QCD Scales

Decouple all particles except dark quarks at a common scale M



Dark QCD Scales



Estimation of Dark Baryon Masses

Require non-perturbative tools like Lattice QCD

Following the analysis of the Cornwall, Jackiw, Tomboulis effective potential for chiral symmetry breaking, one has

$$\alpha_d C_2(R_f) > \pi/3 \quad \alpha_d > \pi/4$$

Using this condition to approximately determine the confinement scales, we have

$$m_p \approx 1.5\Lambda_{\text{QCD}}$$

so,

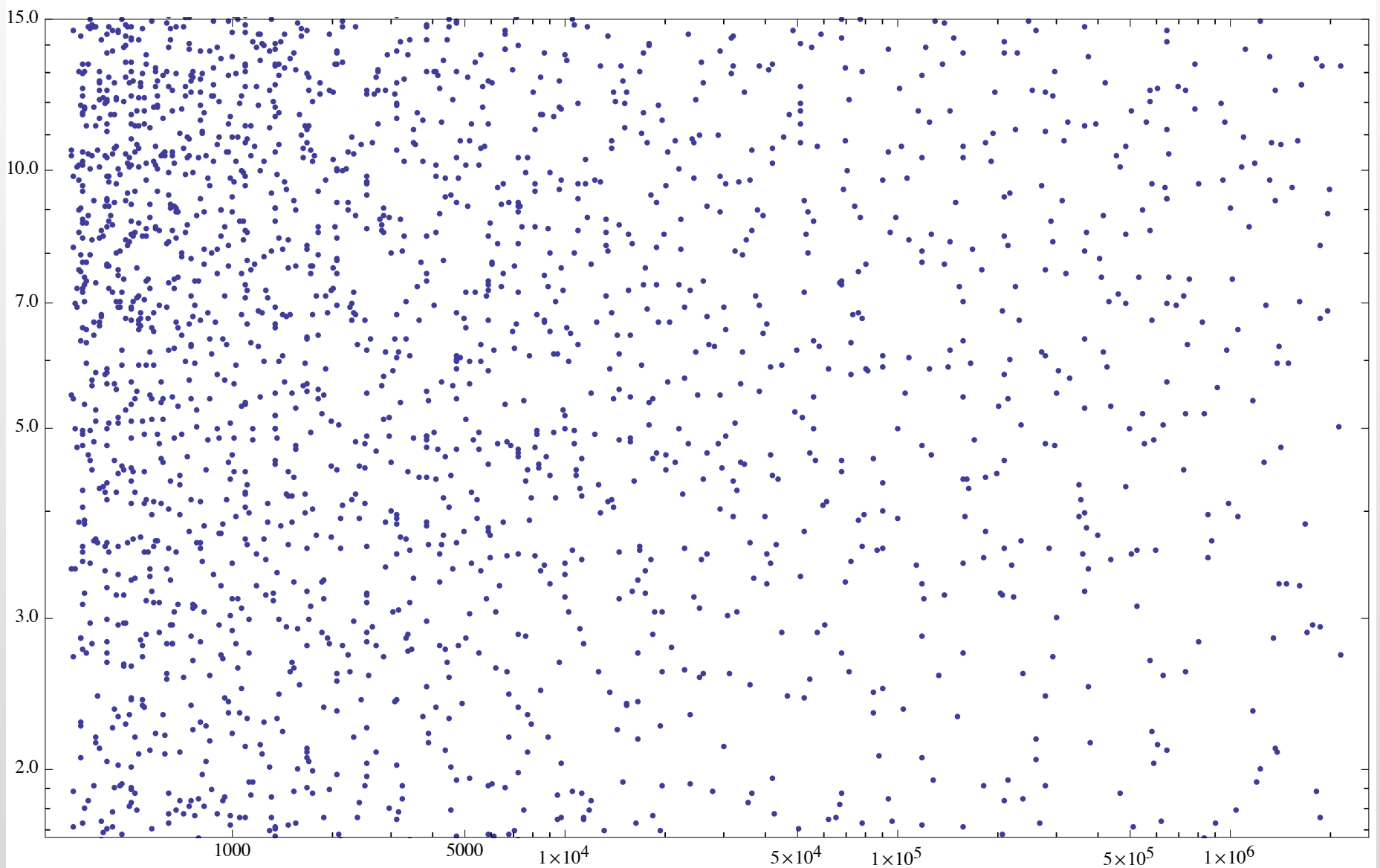
$$m_D \approx 1.5\Lambda_{\text{dQCD}}$$

Lattice inputs
required

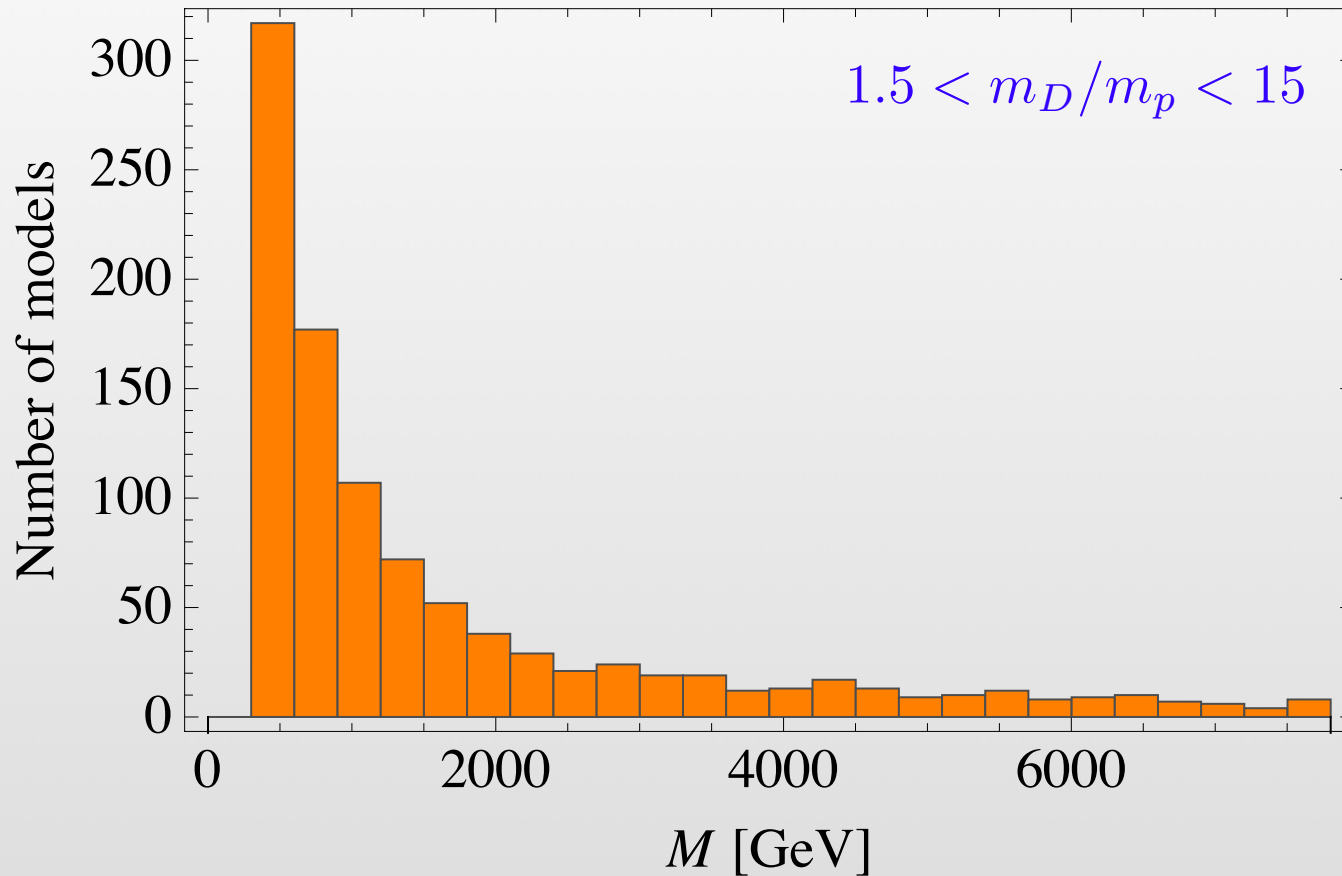
A Sample of Representations

Model	n_{f_c}	n_{f_d}	n_{f_j}	n_{s_c}	n_{s_d}	n_{s_j}	α_s^*	α_d^*	M (GeV)	m_D (GeV)
A	6	5	3	0	2	0	0.095	0.175	518	31
B	6	6	3	1	0	0	0.083	0.120	2030	8.6
C	6	6	3	2	2	0	0.070	0.070	13500	0.32
D	7	7	2	2	0	2	0.078	0.168	3860	72
E	7	7	2	2	1	2	0.090	0.133	869	3.5
F	8	8	2	2	0	1	0.074	0.149	7700	29
G	8	8	2	2	1	1	0.082	0.118	2244	1.2

Many Models



Statistic Distribution of M



The bi-fundamental of QCD and dark QCD prefers to have masses below 2 TeV

Example Model for Number Density

$$(I): \quad n_{\text{DM}} \sim n_p$$

The general idea: generating asymmetry for the bi-fundamental particles

$$\Phi : (\bar{3}, 3)_{1/3}$$

The baryon and dark baryon have comparable number densities from its decay

$$\Phi \rightarrow X_L \bar{d}_R$$



$$n_D \sim n_p$$

Asymmetry of the bi-fundamental

$$\mathcal{L} \supset k_i \bar{Y}_1 \Phi N_i + \text{h.c.}.$$

Generate number asymmetries for $\Delta n_\Phi = -\Delta n_{Y_1}$

$$\epsilon = \frac{\Gamma(N_1 \rightarrow Y_1 \Phi^\dagger) - \Gamma(N_1 \rightarrow \bar{Y}_1 \Phi)}{\Gamma(N_1 \rightarrow Y_1 \Phi^\dagger) + \Gamma(N_1 \rightarrow \bar{Y}_1 \Phi)} \approx -\frac{3}{2} \frac{1}{8\pi} \frac{\Im m[k_1^2 (k_2^*)^2]}{|k_1|^2} \frac{M_1}{M_2}$$

$$\mathcal{L} \supset \kappa_1 \Phi \bar{Y}_1^c Y_2 + \kappa_2 \Phi \bar{Y}_2 e_R + \kappa_3 \Phi \bar{X}_L d_R + \text{h.c.},$$

$$Y_1 \rightarrow \bar{Y}_2 \Phi^\dagger \quad Y_2 \rightarrow \Phi e_R$$



$$\Delta n_\Phi = -3\Delta n_{Y_1}$$

Asymmetries of Baryon and Dark Baryon

Without weak interaction and electroweak sphaleron processes

$$\begin{aligned} \Phi \rightarrow X_L \bar{d}_R &\longrightarrow \Delta n_{d_R} \equiv 3 n_B = 3 \Delta n_{Y_1} , \\ &\Delta n_{e_R} \equiv n_L = -\Delta n_{Y_1} , \\ &\Delta n_X \equiv 3 n_D = -3 \Delta n_{Y_1} , \end{aligned}$$

After taking the weak processes into account

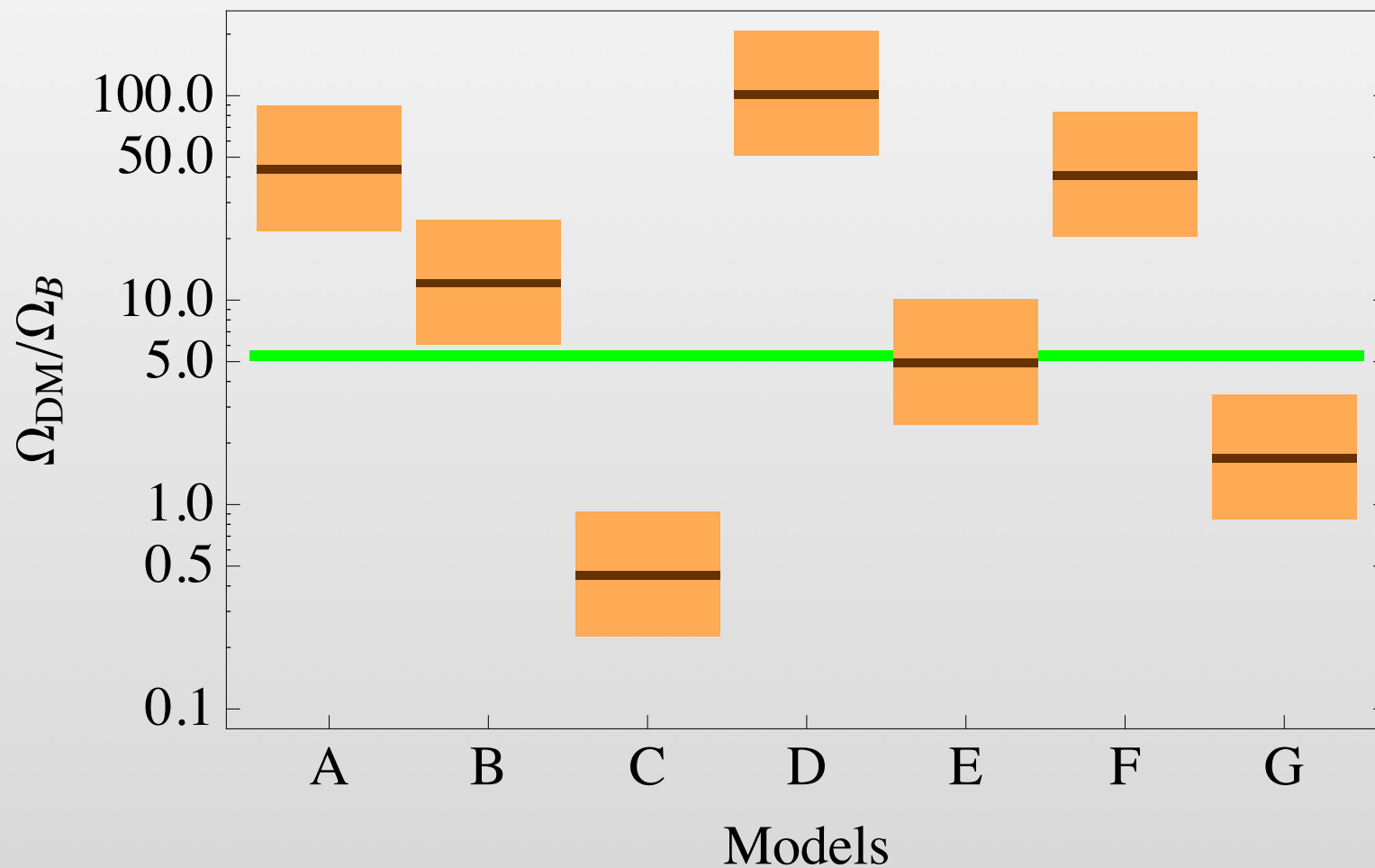
$$n_B = \frac{28}{79} n_{B-L}$$

Chung, Garbrecht, Tulin
arXiv:0807.2283

$$\downarrow$$
$$\frac{|n_D|}{n_B} = \frac{79}{56}$$

Ratios of Energy Densities

$$\frac{\Omega_{\text{DM}}}{\Omega_{\text{Baryon}}} = \frac{n_D m_D}{n_B m_p} \approx \frac{79}{56} \frac{m_D}{m_p}$$



Dark Matter Phenomenology

All relevant phenomenology depends on the bi-fundamental particles, which have a mass at 1-2 TeV

Integrate out the Φ field

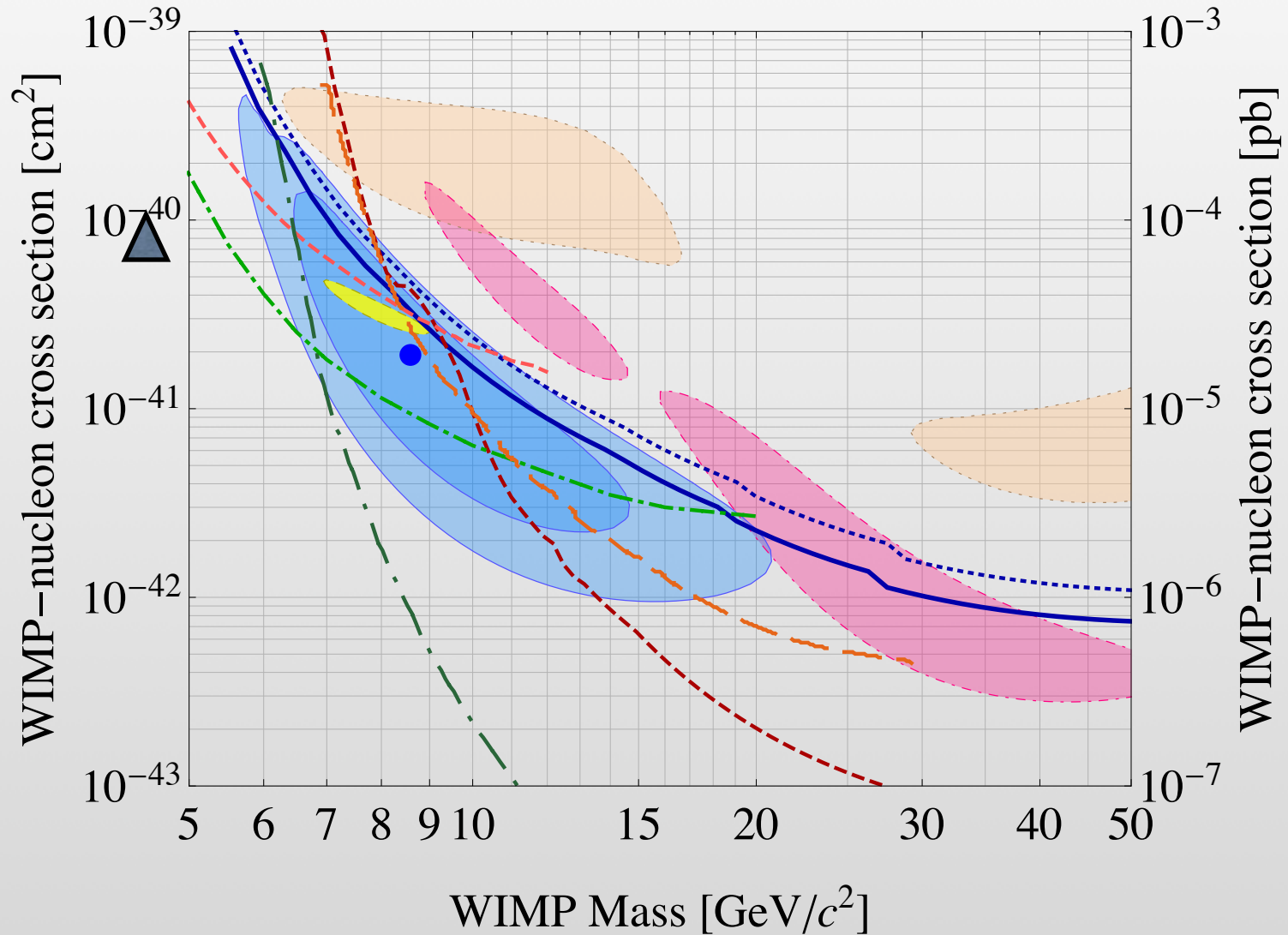
$$\frac{\kappa_3^2 \bar{X}_L \gamma_\mu X_L \bar{d}_R \gamma^\mu d_R}{M_\Phi^2}$$

Spin-independent dark baryon-neutron cross section

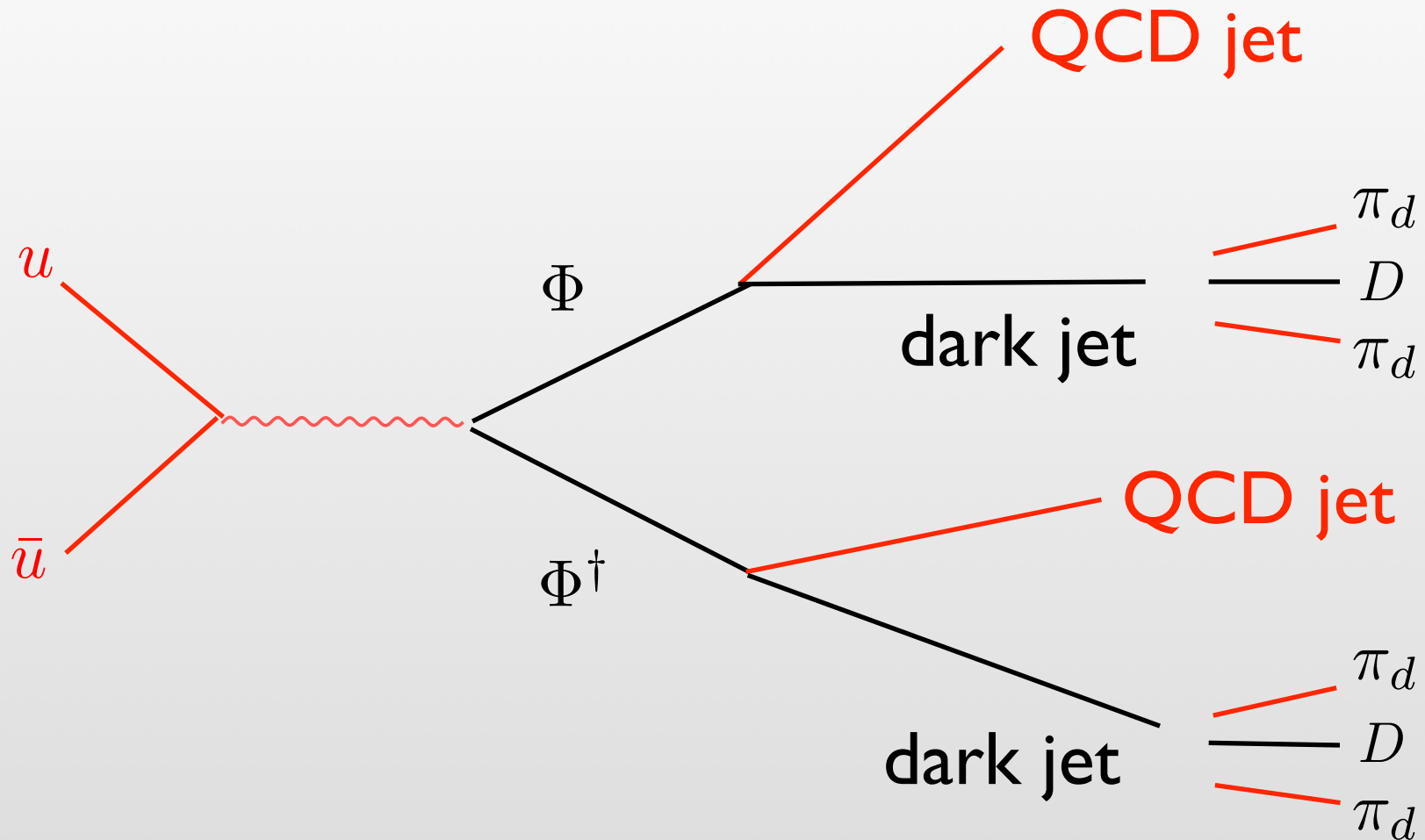
$$\sigma_{D-n}^{\text{SI}} = \frac{2^2 3^2 \kappa_3^4 \mu_{D-n}^2}{16 \pi M_\Phi^4} = \left(\frac{1 \text{ TeV}}{M_\Phi / \kappa_3} \right)^4 \times 3 \times 10^{-40} \text{ cm}^2$$

Dark Matter Phenomenology

CDMS, I 304.4279



Collider Phenomenology



missing energy is dramatically reduced

Conclusions

- ★ Thermal dark neutron points to the dark QCD scale to be ~ 100 TeV. The direct detection depends on the explicit models of how to relate the dark sector to our sector
- ★ For asymmetry DM models, infrared fixed points can relate the QCD and dark QCD confinement scales and explain why dark baryon masses are at the same scale with the proton mass
- ★ More inputs from Lattice are required to calculate coefficients of order of unit

Thanks